



## Spectrum of (eventually) positive semigroups

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**Keywords:** One-parameter semigroup of linear operators; positive semigroups; eventually positive semigroup; long-term behaviour; stability.

**MSC2010 codes:** 47D06, 47B65, 47A10

**Introduction.** It is well-known that the growth bound and spectral bound of the generator of a positive  $C_0$ -semigroup on  $E$  coincide if  $E = L^p(\Omega)$  for  $p \in [1, \infty]$ ,  $C(K)$  for a compact Hausdorff set  $K$ , or  $C_0(\Omega)$  for a locally compact Hausdorff space  $\Omega$ . However, the previously known proofs are quite technical in nature. Recently, Hendrik Vogt gave a much shorter proof of the result for  $L^p$ -spaces. Inspired by his ideas, we present a simple proof of the result for the spaces of continuous functions. In fact, the proof can also be adapted to the more general class of *eventually positive semigroups*. We use this as a motivation to look at some other spectral properties of eventual positivity.

### References

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